

## *Supplementary Material*

### **Text S1:**

The specific formula for calculating the analytical solution for diffuse transport in the target area of aircraft catalytic operations is as follows:

$$q(x, y, z, t) = \sum_{n=1}^k q_n(x, y, z, t) (k: t_{n=k} < t < t_{n=k+1})$$

$$q_n(x, y, z, t) = \frac{Q_n}{8\sqrt{\pi^3 k_H^2 k_v} (t - t_n + t^*)^3}$$

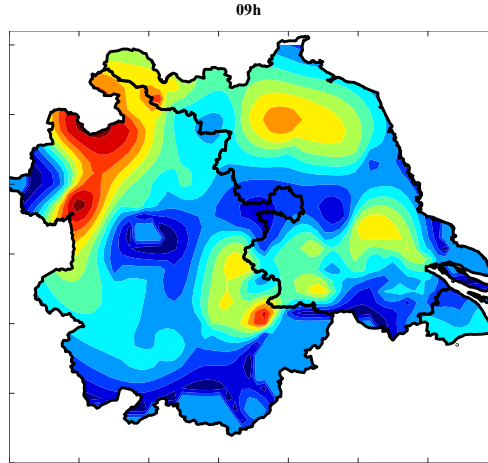
$$\times e^{-\frac{[x-x_n-u(t-t_n)]^2}{4k_H(t-t_n+t^*)}} e^{-\frac{[y-y_n-v(t-t_n)]^2}{4k_H(t-t_n+t^*)}} e^{-\frac{[z-z_n-\omega(t-t_n)]^2}{4k_v(t-t_n+t^*)}}$$

$$\ln q_n = \ln Q_n - \ln 8 - \frac{3}{2} \ln \pi - \ln k_H - \frac{1}{2} \ln k_v - \frac{3}{2} \ln(t - t_n + t_0)$$

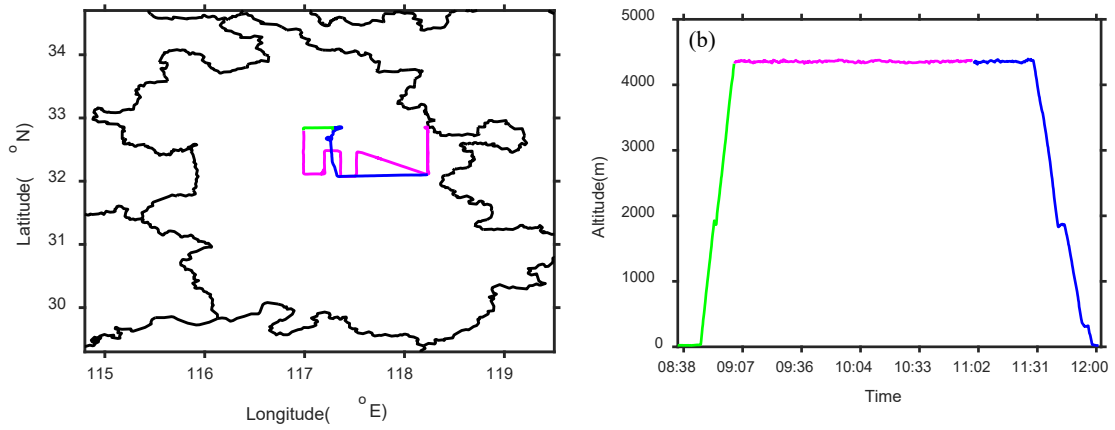
$$- \frac{[x - x_n - u(t - t_n)]^2}{4k_H(t - t_n + t_0)} - \frac{[y - y_n - v(t - t_n)]^2}{4k_H(t - t_n + t_0)}$$

$$- \frac{[z - z_n - \omega(t - t_n)]^2}{4k_v(t - t_n + t_0)}$$

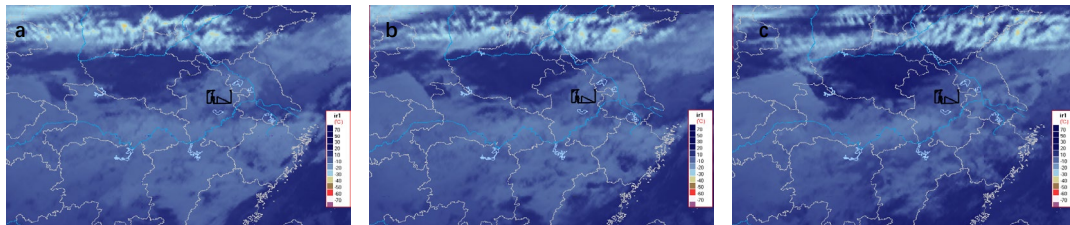
where  $q$  is the diffuse material concentration;  $u$ ,  $v$ , and  $\omega$  represent the fractional wind speeds on the  $x$ ,  $y$ , and  $z$  axes, respectively;  $k_H$  and  $k_v$  are the turbulence coefficients in the horizontal and vertical directions, respectively.  $t$  is time. The seeding volume is  $Q_n = R\Delta t$ , where  $R$  is the seeding rate in g/s.  $x_n$ ,  $y_n$ ,  $z_n$ , and  $t_n$  are the four-dimensional exact coordinates of the  $n$ th aircraft seeding point, which are input from the aircraft GPS real measurements.



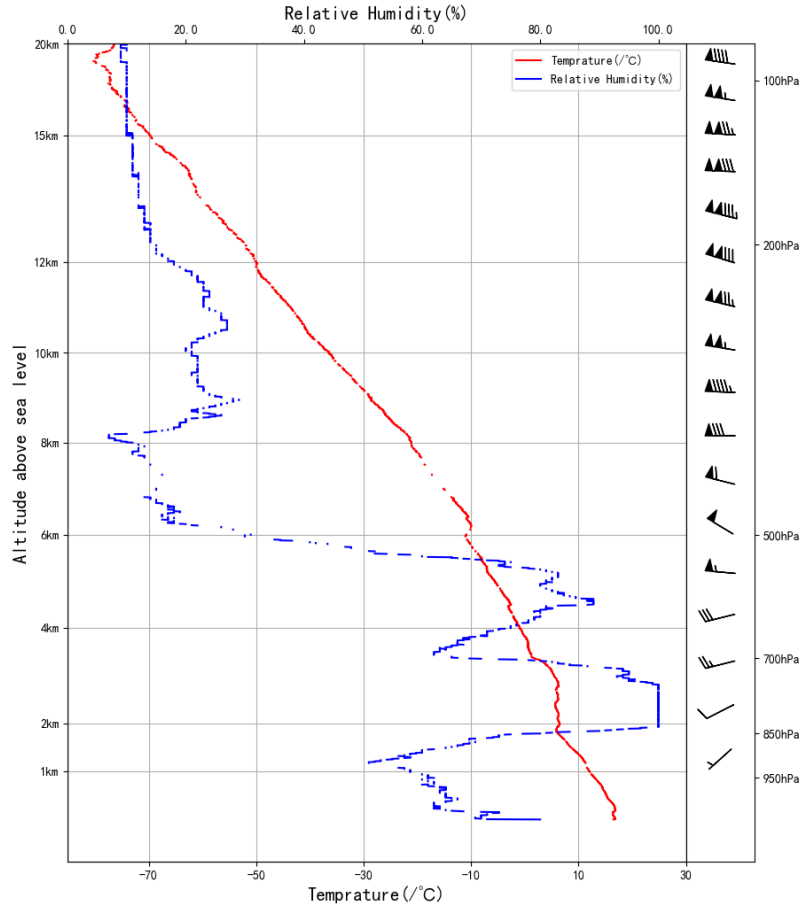
**Figure S1.** The spatial distribution of PM<sub>2.5</sub> mass concentration at 09:00 on November 01, 2020.



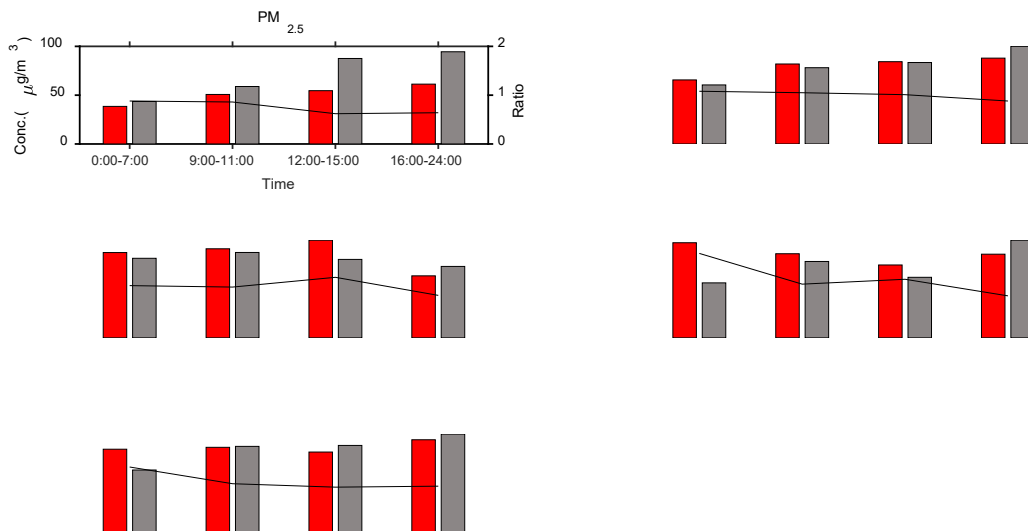
**Figure S2.** (a) Flight track and (b) altitude during the precipitation enhancement operation on November 1, 2020 (the green segment is the take-off and climbing stage, the purple segment (09:00-11:10) is the operation stage (AgI seeding), and the blue segment is the return stage after operation )



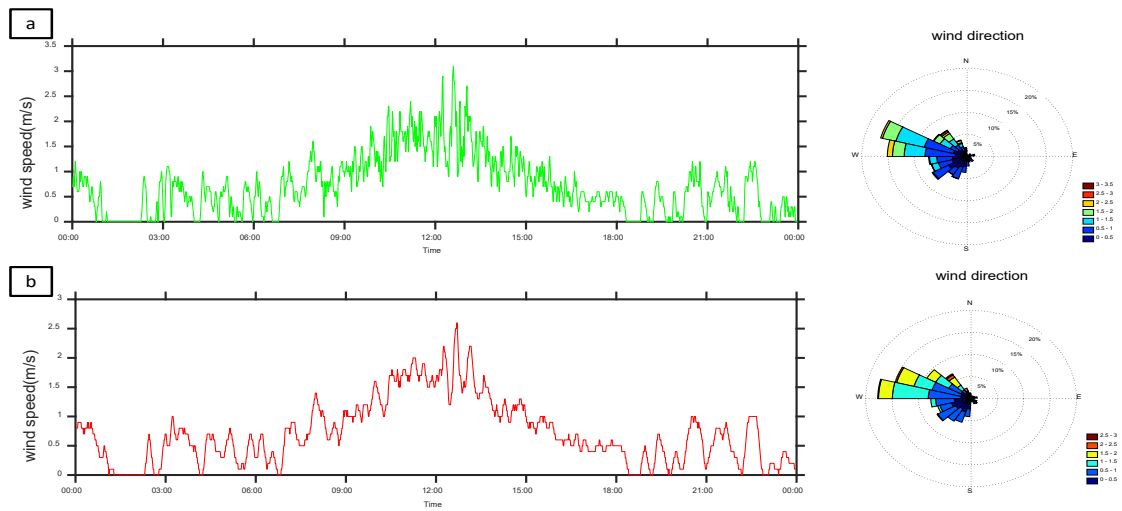
**Figure S3.** 10.8  $\mu\text{m}$  infrared cloud image at 08:30 BT(a), 09:30 BT(b), 11:30 BT(c) on November 1, 2020 from the FY-4A satellite.



**Figure S4.** Temperature profile (red solid line), relative humidity profile (blue solid line), and wind speed and direction (black wind) from sounding data in Nanjing at 08:00 BT on November 1, 2020.



**Figure S5.** The mass concentrations of air pollutants in the target and contrast areas (bar plots) and their ratios (black lines).



**Figure S6.** (a) 2-minute and (b) 10-minute average wind speed and direction at NUIST on November 1, 2020