

# Global Carbon Cycle

## AOSC / CHEM 433 & AOSC 633

### Ross Salawitch & Walt Tribett

Class Web Sites:

<http://www.atmos.umd.edu/~rjs/class/spr2019>

<https://myelms.umd.edu/courses/1256337>

Email:

Ross: [rsalawit@umd.edu](mailto:rsalawit@umd.edu) or [rjs@atmos.umd.edu](mailto:rjs@atmos.umd.edu); Walt: [wtribett@umd.edu](mailto:wtribett@umd.edu)

### Goals for today:

- Overview of the Global Carbon Cycle “scratching below the surface”
- Ocean and land uptake of CO<sub>2</sub>
- Connect to policy and long-term climate change

## Lecture 5

### 14 February 2019

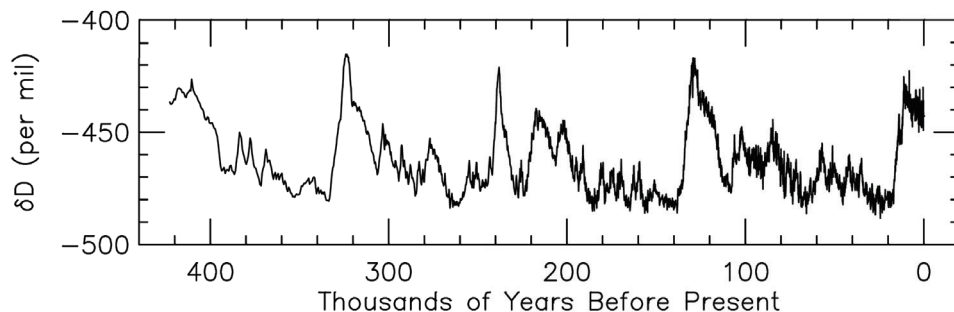
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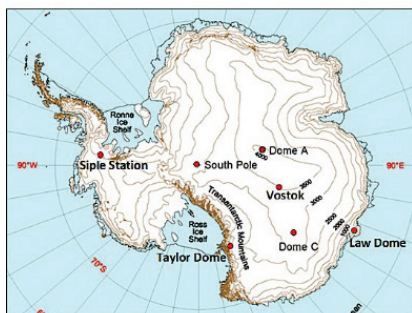
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## Vostok Ice Core

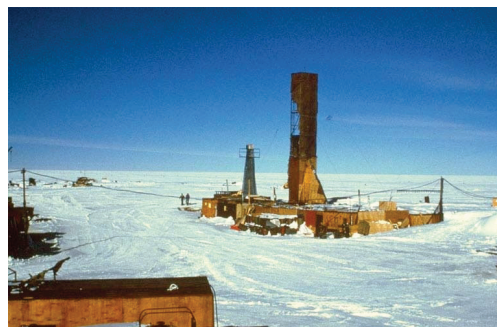
- January 1998: ice core with depth of 3.6 km extracted at Russian Vostok Station, Antarctica
- Vostok ice-core record extends back 400,000 years in time (Petit *et al.*, *Nature*, 1999)
- Reconstructed temperature based on measurement of the deuterium content of ice
- $\delta^{18}\text{O}$  shows tremendous variations in global ice volume (not shown)
- Ice core data show last four ice ages, punctuated by relatively brief interglacials



Vostok Drill



[https://cdiac.ess-dive.lbl.gov/trends/co2/ice\\_core\\_co2.html](https://cdiac.ess-dive.lbl.gov/trends/co2/ice_core_co2.html)



<http://www.astrosurf.com/luxorion/Sciences/vostok-drill.jpg>

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# Problem Set #1 has been modified

Modified 14 Feb 2019 (modifications in **blue bold face**)

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c) (10 points) Compute a new effective temperature for Earth, using the albedo found in part ii of Q1b.

d) (10 points) Compare the two effective temperatures found in a) and c), and state whether:

i) the difference is physically consistent with the direction implied by the change in Earth's albedo that would result from a massive loss of sea-ice

ii) you think your calculations support the notion **that the “positive feedback”: that is, a response (melting ice) to a driver (global warming) that re-inforces the initial action (warming) called the “ice-albedo” effect is a potentially important process.**

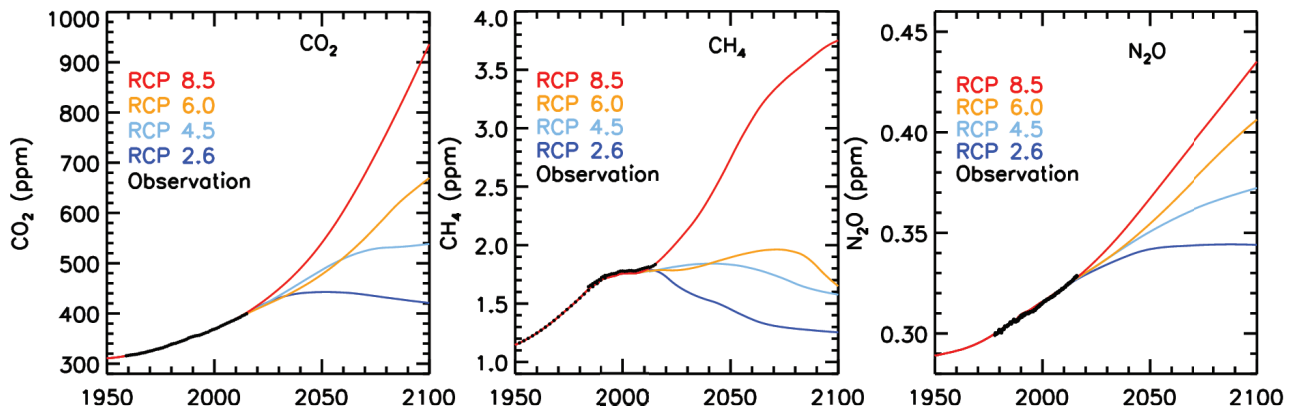
Note: there is also genuine concern about the impact of melting Arctic sea ice on the habitat for polar bears and the ecology of the Arctic. For ii) of this question, we would like your focus to be on the numerical calculations you have conducted.

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## Motivation 1



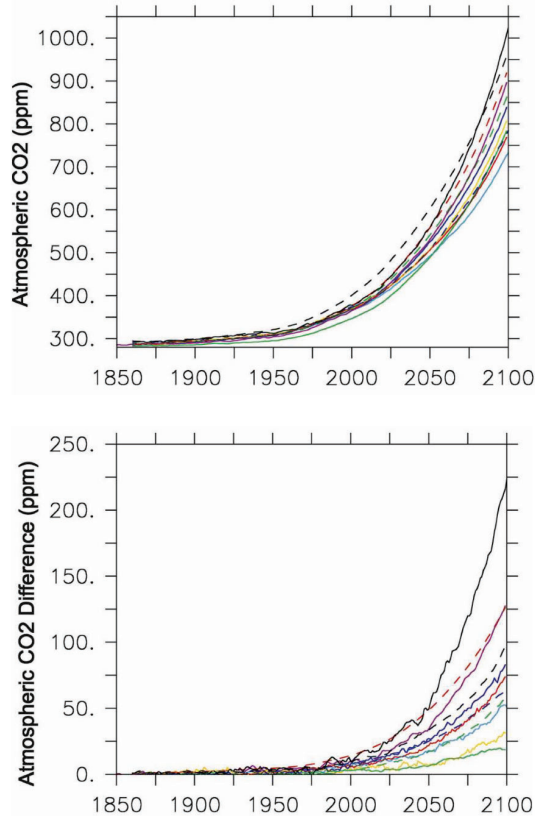
- RCP: Representative Concentration Pathway  
Number represents  $\Delta RF$  of climate ( $W m^{-2}$ ) at the end of this century
- GHG mixing ratio time series for  $CO_2$ ,  $CH_4$ ,  $N_2O$ , as well as CFCs, HCFCs, and HFCs that are provided to climate model groups

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## Motivation 2



- Prior slide examined atmospheric CO<sub>2</sub> from a single model of the global carbon cycle
- Friedlingstein et al. (2006) compared CO<sub>2</sub> from **11** different coupled climate-carbon cycle models, each constrained by the same specified time series of anthropogenic CO<sub>2</sub> emission and found:
  - 1) future climate change will reduce the efficiency of the *Earth system* to absorb the anthropogenic carbon perturbation
  - 2) difference in CO<sub>2</sub> between a simulation using an interactive carbon-cycle and another run with a non-interactive carbon-cycle varies from 20 to 200 ppm among these **11** models (yikes!)

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**CO<sub>2</sub> is long lived: society must reduce emissions soon or we will be committed to dramatic, future increases in [CO<sub>2</sub>]**

**Curves for which [CO<sub>2</sub>] levels off at ~550 ppm or less have emissions peaking NOW !**

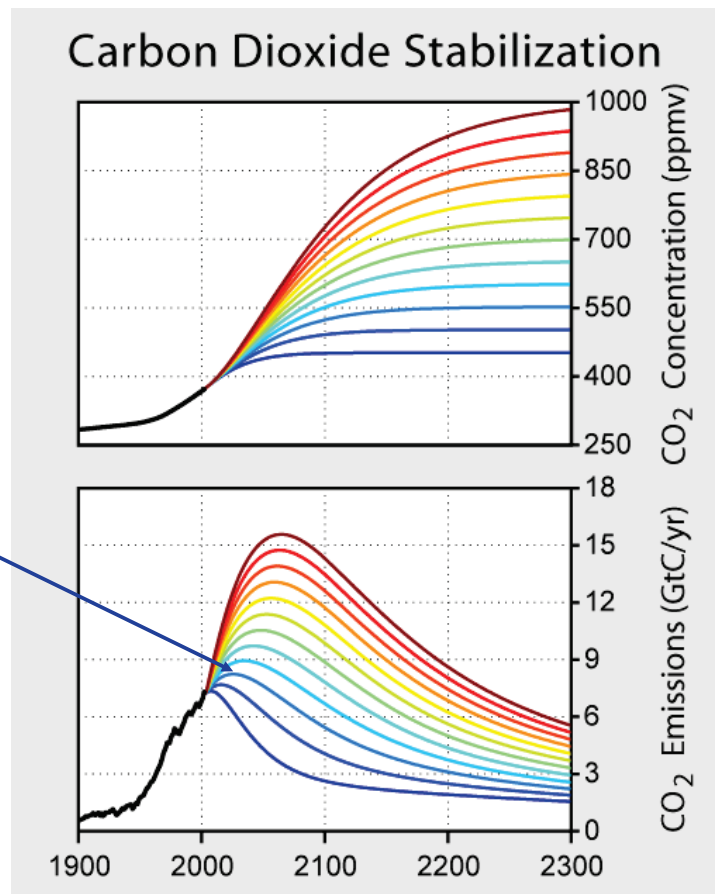
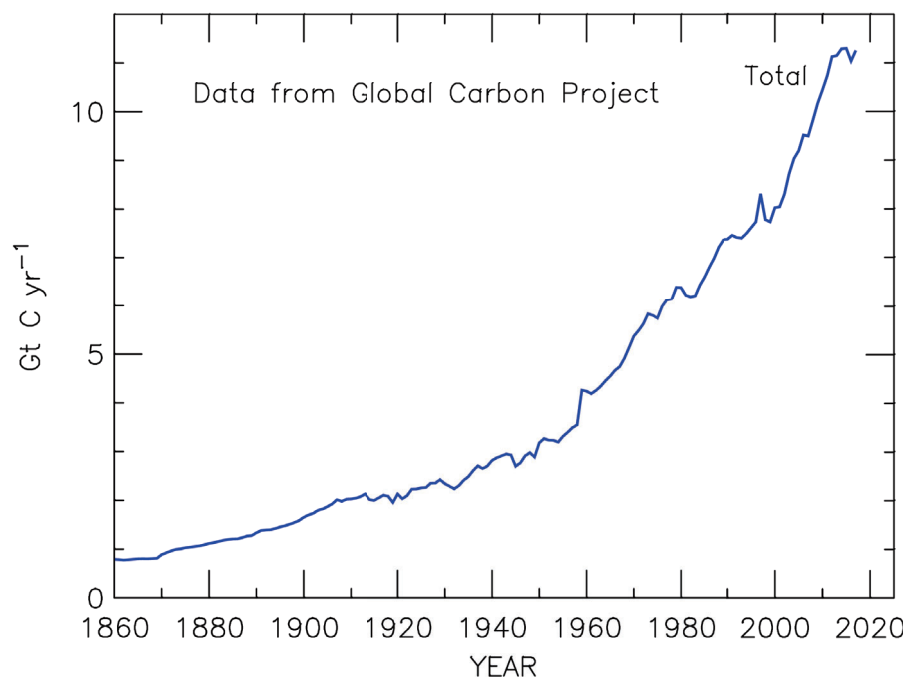


Image: "Global Warming Art" : <http://archive.is/JT5rO>

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## Fossil Fuel, Cement, and Land Use Change Emissions 1860 to Present



Note: Gt is an abbreviation for giga tons, or  $10^9$  tons. Here we are using metric tons:  
**1 metric ton =  $10^3$  kg ; therefore, 1 Giga ton =  $10^{15}$  g, where g is grams.**

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## Modern CO<sub>2</sub> Record

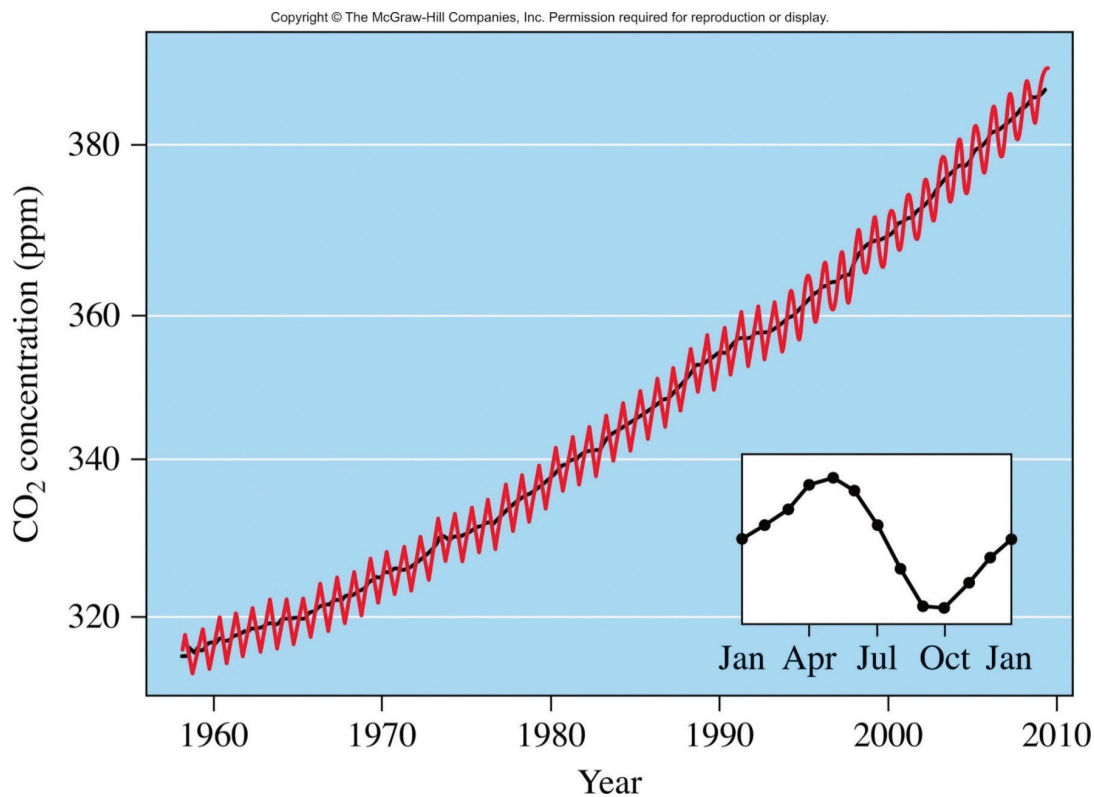


Figure 3.3, Chemistry in Context

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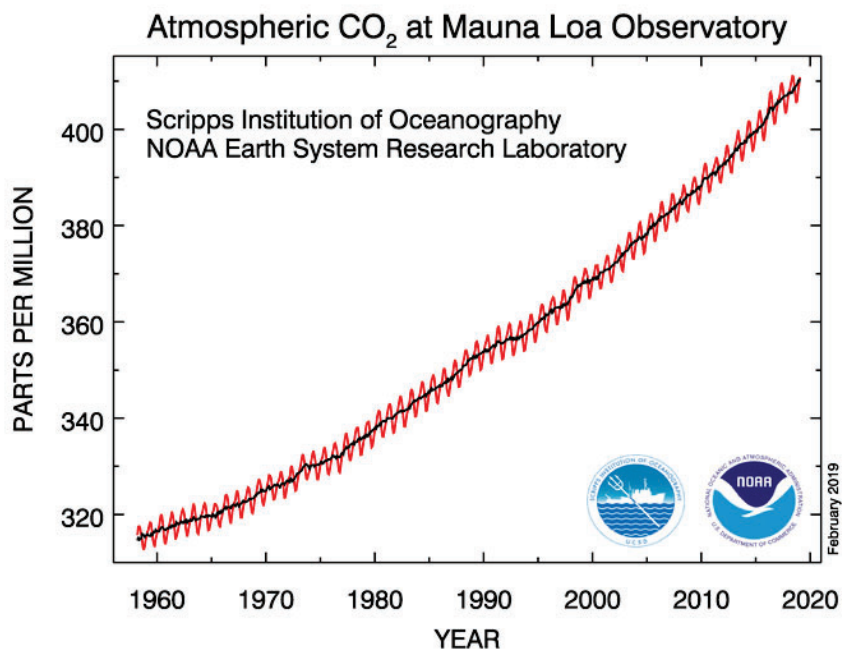
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## Modern CO<sub>2</sub> Record

CO<sub>2</sub> at MLO on 7 Feb 2017: 406.7 parts per million (ppm)

CO<sub>2</sub> at MLO on 12 Feb 2019: 411.8 parts per million (ppm)



Legacy of Charles Keeling, Scripps Institution of Oceanography, La Jolla, CA

<https://www.esrl.noaa.gov/gmd/ccgg/trends/full.html>

See also <https://www.co2.earth/daily-co2>

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## Modern CO<sub>2</sub> Record

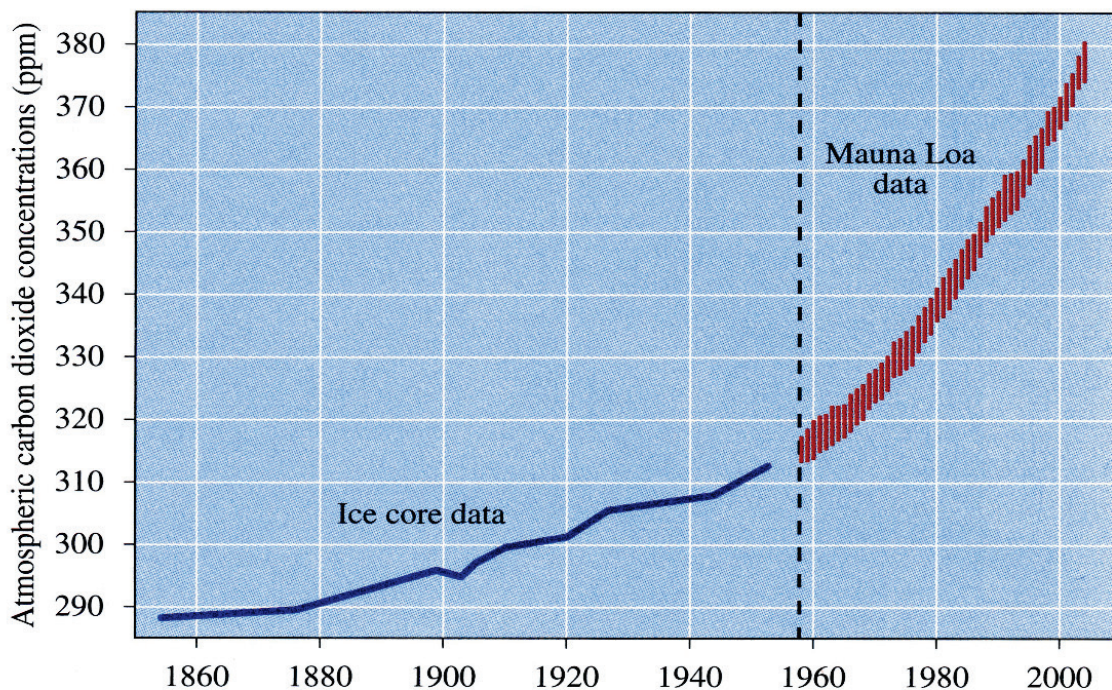


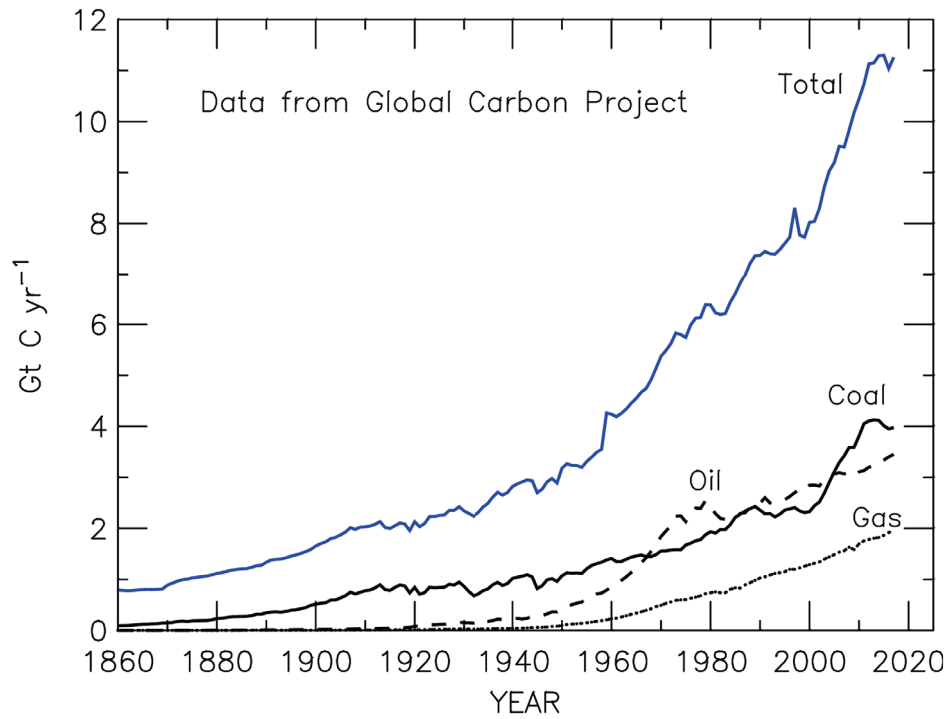
Figure 3.5, *Chemistry in Context*, 6<sup>th</sup> Edition

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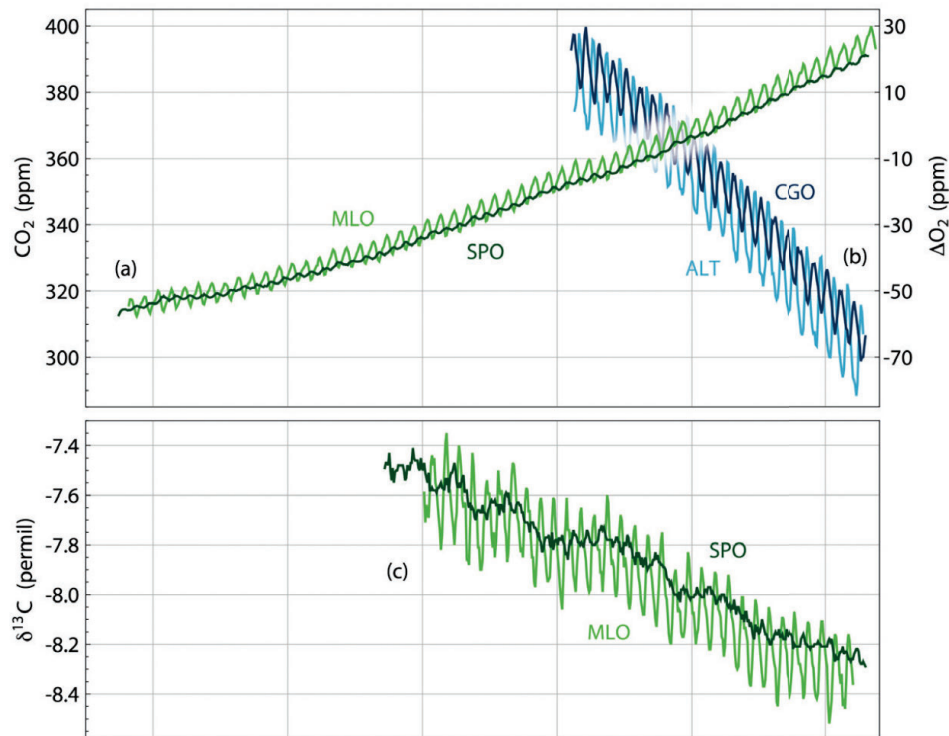
# Fossil Fuel, Cement, and Land Use Change Emissions 1860 to Present



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## Human “Fingerprints” on Atmospheric $\text{CO}_2$



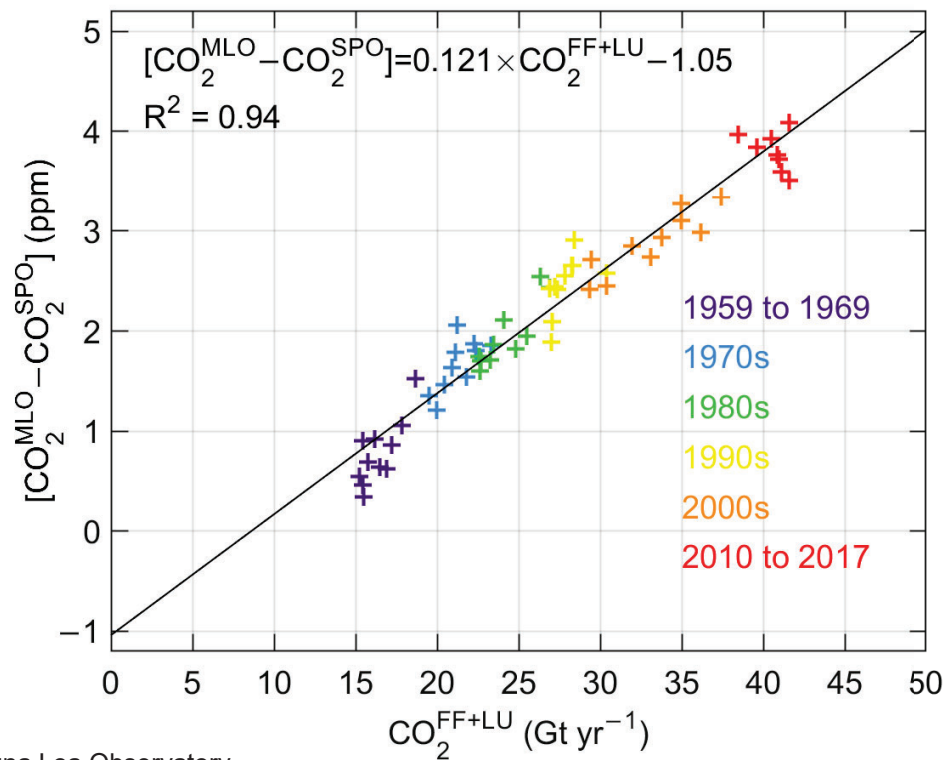
**Figure 3.4** Atmospheric concentrations observed at representative stations of (a) carbon dioxide from Mauna Loa (MLO) Northern Hemisphere and South Pole (SPO) Southern Hemisphere; (b) Oxygen from Alert (ALT) Canada, 82°N, and Cape Grim (CGO), Australia, 41°S; (c)  $^{13}\text{C}/^{12}\text{C}$  from Mauna Loa (MLO) and South Pole (SPO) stations.

**Fig 3.4, Houghton**

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# Human “Fingerprints” on Atmospheric CO<sub>2</sub>



MLO: Mauna Loa Observatory  
 SPO: South Pole Observatory

Fig 1.8 updated, *Paris Beacon of Hope*

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Note, here we use Gt C, whereas in the book, we used GT CO<sub>2</sub>

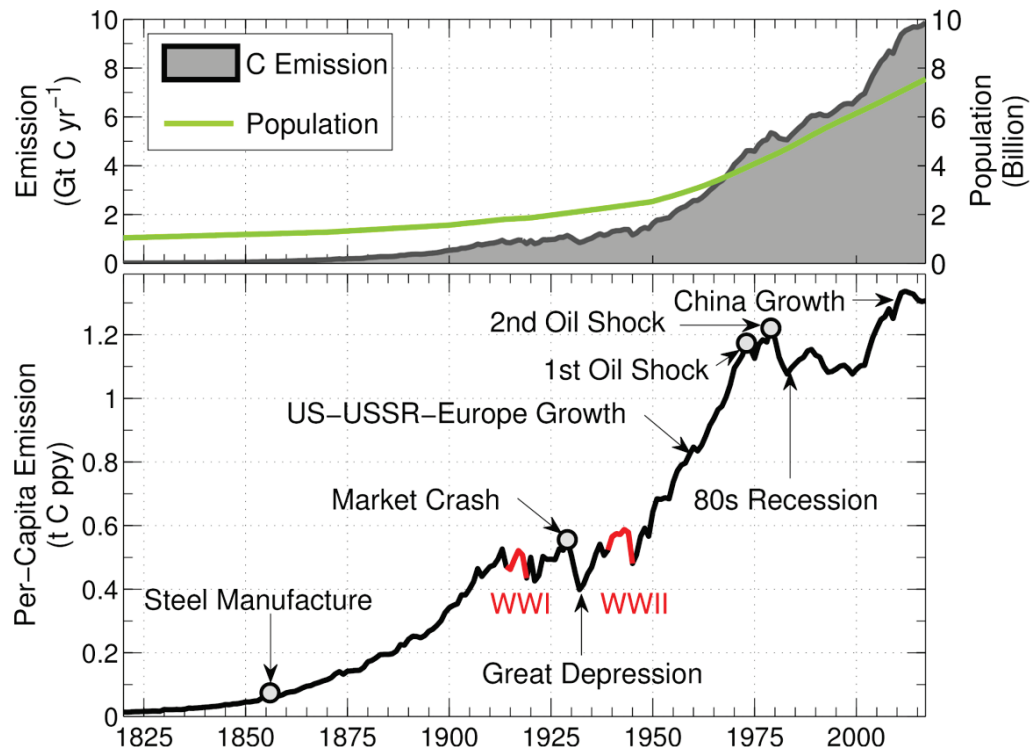


Figure courtesy Walt Tribett

After Fig 3.1 *Paris Beacon of Hope*

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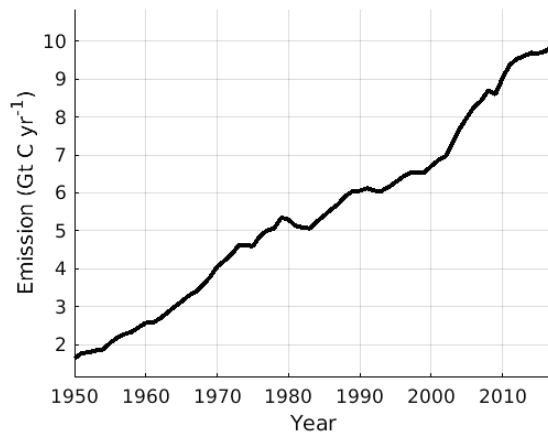
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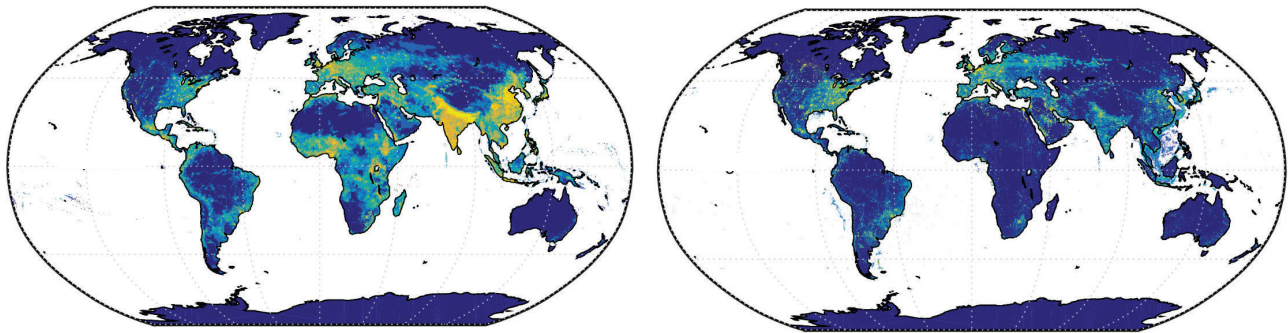
# Fossil Fuel Emissions

Global Carbon Emission Increase 1950-2017



Fossil fuel emissions, 1950 = **1.6** Gt C  
2017 = **9.9** Gt C

What are the primary social factors driving factors responsible for this rise?



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## Obama & Xi

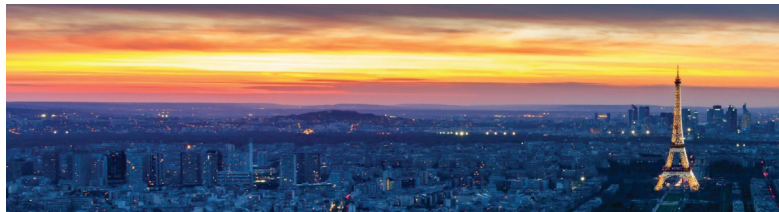
### US / China Announcement ⇒ Paris Climate Agreement



Nov 2014: Presidents Obama & Xi announced

U.S. would reduce GHG emissions to **27%** below 2005 **by 2025**

China would **peak** GHG emissions **by 2030** with best effort to peak early



### Paris Climate Agreement:

Article 2, Section 1, Part a):

Objective to hold “increase in GMST to well below **2°C** above pre-industrial levels and to pursue efforts to limit the temperature increase to **1.5°C** above pre-industrial levels”

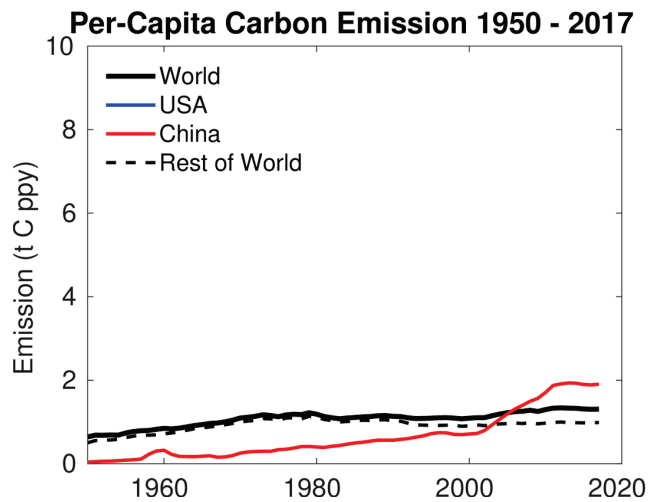
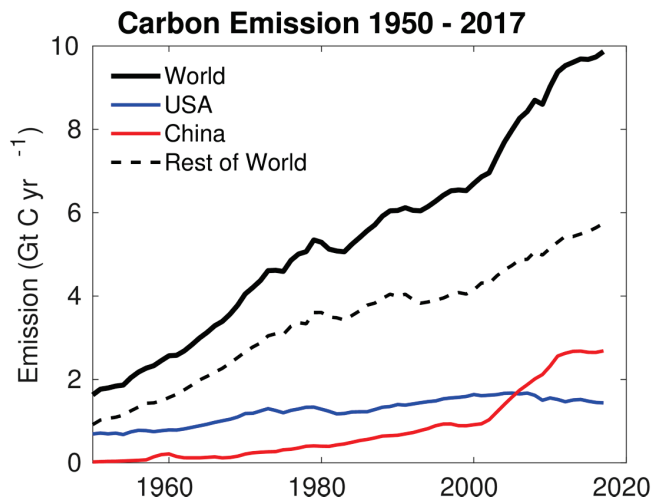
### NDC: Nationally Determined Contributions to reduce GHG emissions

- Submitted prior to Dec 2015 meeting in Paris
- Consist of either **unconditional** (promise) or **conditional** (contingent) pledges
- Generally extend from early 2016 to year 2030

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Figures courtesy Walt Tribett

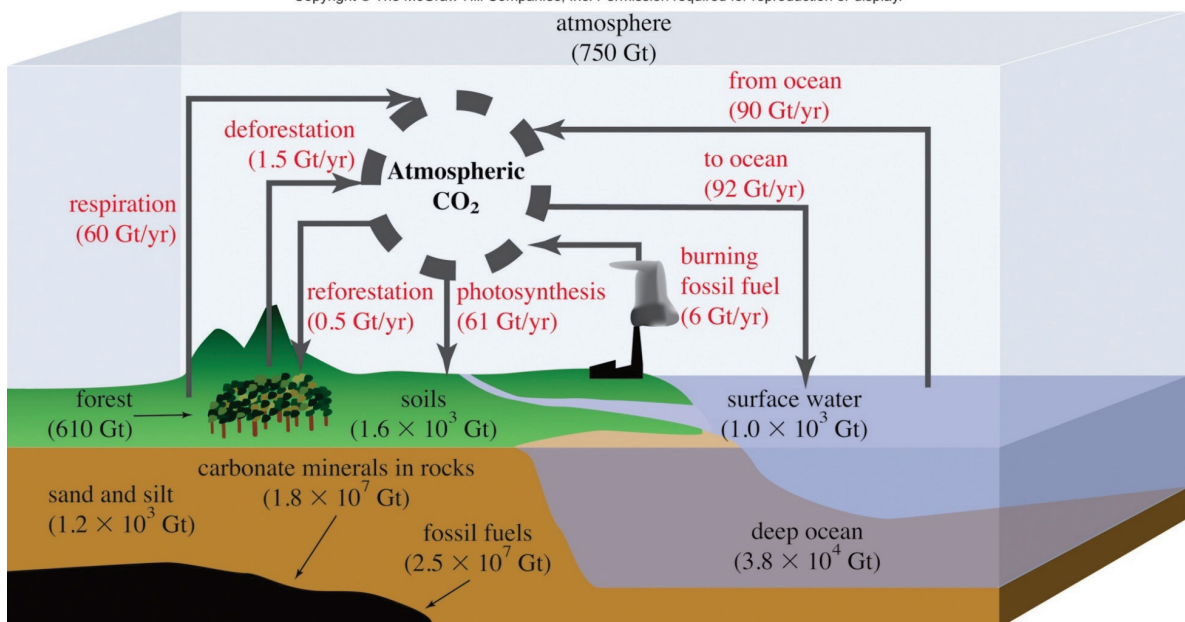
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## Global Carbon Cycle

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Ocean Carbon:  $1.0 \times 10^3 \text{ Gt} + 3.8 \times 10^4 \text{ Gt} = 3.9 \times 10^4 \text{ Gt}$

Fig 3.20, Chemistry in Context

Ocean contains ~50 times more Carbon than the atmosphere

$$\begin{aligned} \text{Mass of C (in CO}_2\text{)} &= 409.5 \times 10^{-6} \times 5.27 \times 10^{21} \text{ grams} \times \left\{ \frac{12 \text{ grams/mole}}{28.8 \text{ grams/mole}} \right\} \\ &= 899 \times 10^{15} \text{ grams or } 899 \text{ Gt} \end{aligned}$$

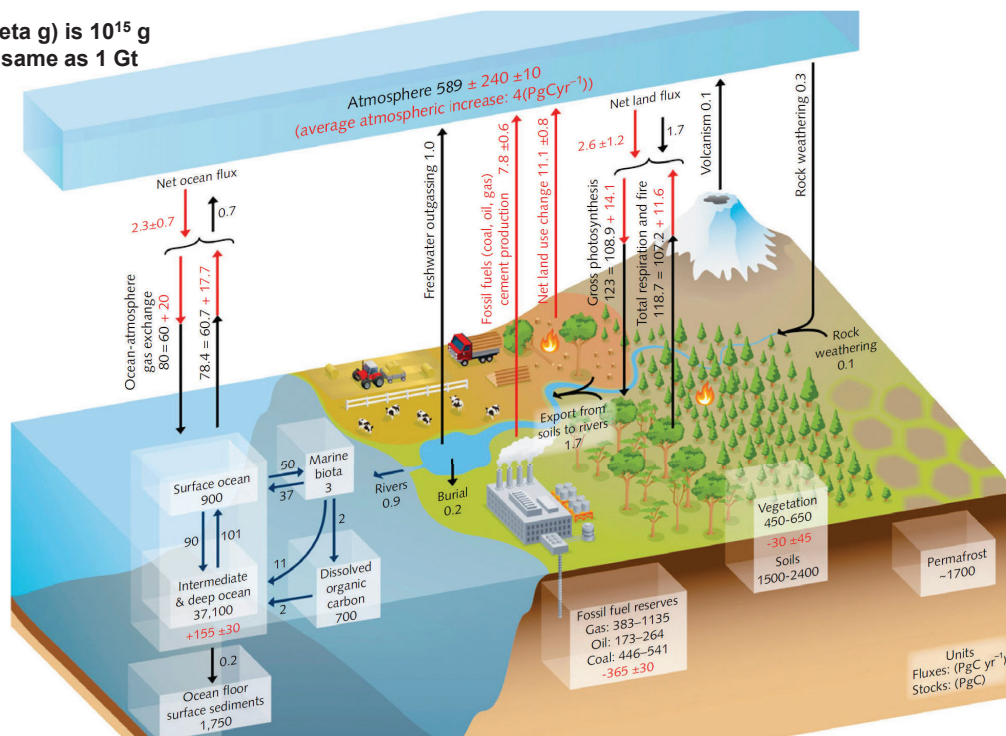
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Note: 1 Pg (peta g) is  $10^{15}$  g  
exactly the same as 1 Gt



Houghton:

Land Sink =  $2.6 \pm 1.2$  Gt C / yr  
Ocean Sink =  $2.3 \pm 0.7$  Gt C / yr

Fig 3.1, Houghton

In other words,  $\sim 4.9$  Gt C / yr out of  $7.8 + 1.1 = 8.9$  Gt C / yr from burning fossil fuel & deforestation is being absorbed by world's oceans & terrestrial biosphere for the time period of this figure, which is 2000 to 2009

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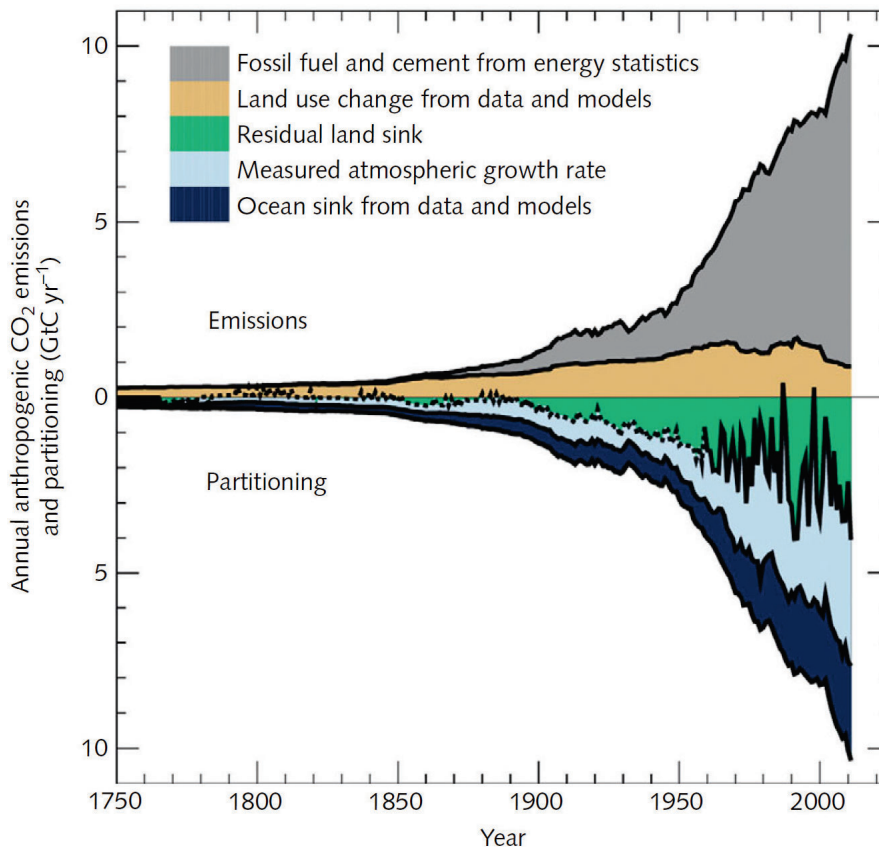


Fig 3.3, Houghton

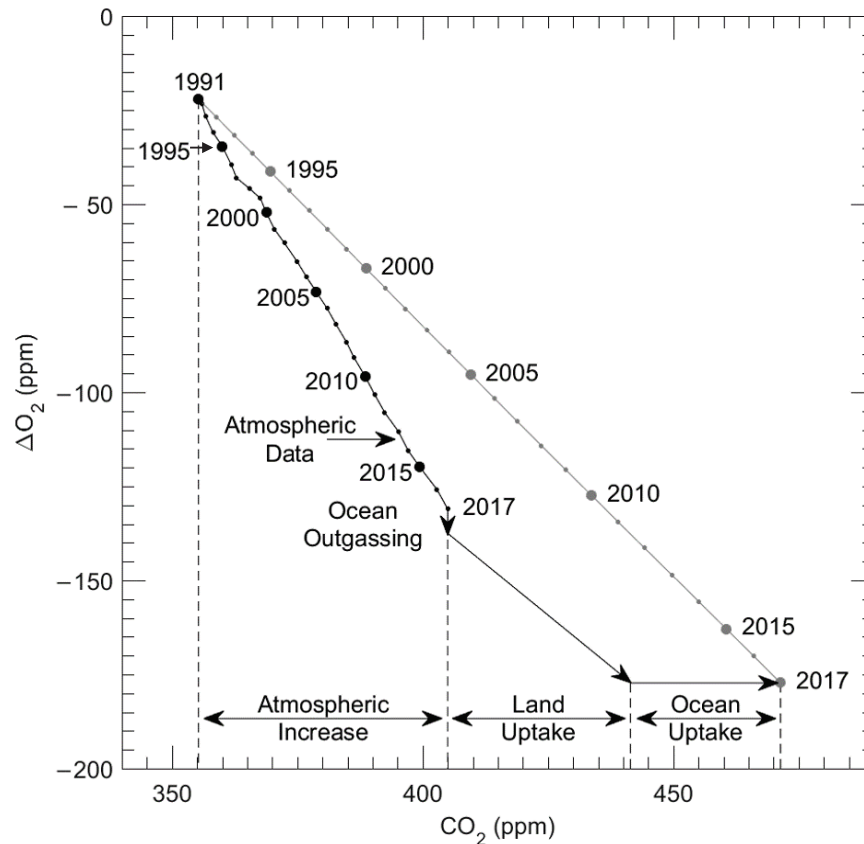
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## Inferring CO<sub>2</sub> Uptake Based on $\Delta O_2$

Figure courtesy  
Brian Bennett



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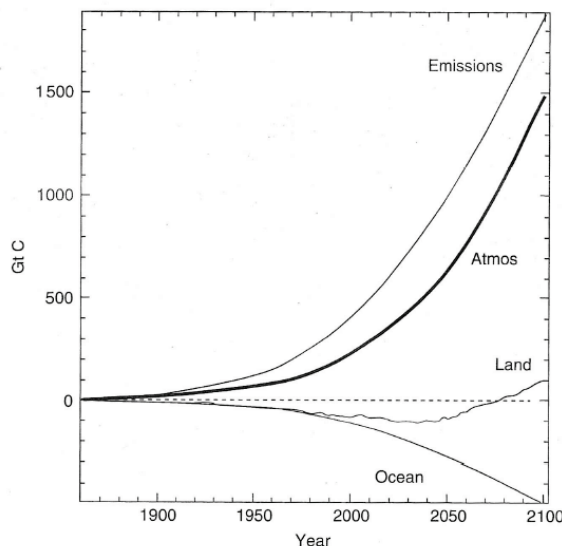
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## Uptake of Atmospheric CO<sub>2</sub> by Trees (Land Sink)

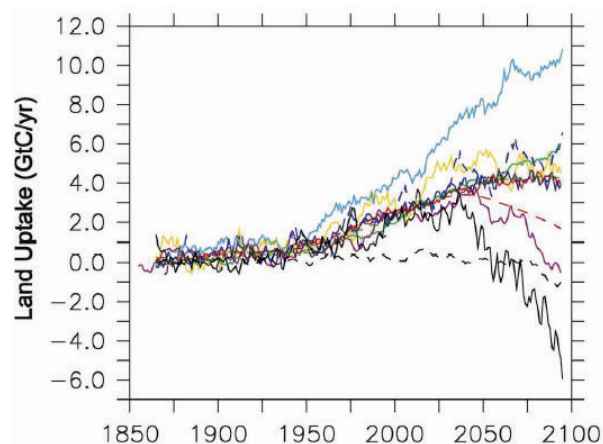
Land sink: relatively short lived reservoir

- In this model, future water stress due to climate change eventually limits plant growth
- Feedbacks between climate change & plants could lead to almost 100 ppm additional CO<sub>2</sub> by end of century



**Figure 3.5** Illustrating the possible effects of climate feedbacks on the carbon cycle. Results are shown of the changing budgets of carbon

- Future fate of land sink highly uncertain according to [11](#) coupled climate-carbon cycle models examined by Friedlingstein et al. (2006)



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# Uptake of Atmospheric CO<sub>2</sub> by Trees (Land Sink)

## Land sink

Recently launched instrument will use a lidar to map global vegetation



### GEDI: Global Ecosystem Dynamics Investigation



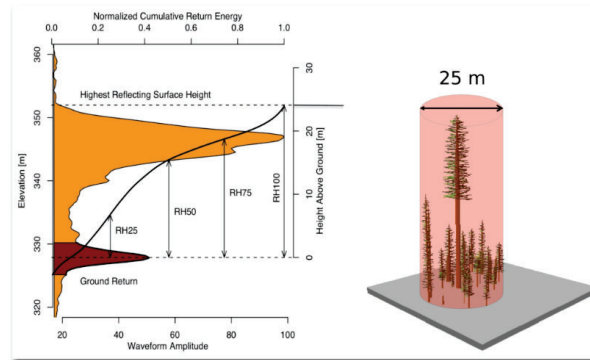
MISSION INSTRUMENT SCIENCE APPLICATIONS DATA NEWS/EDUCATION

#### LEVEL 1 - GEOLOCATED WAVEFORMS

The raw GEDI waveforms as collected by the GEDI system are geolocated by our science team.

#### LEVEL 2 - FOOTPRINT LEVEL CANOPY HEIGHT AND PROFILE METRICS

The waveforms are processed to provide canopy height and profile metrics. These are values calculated directly from the waveform return for each footprint such as terrain elevation, canopy height, RH metrics and Leaf Area Index (LAI). These metrics provide easy-to-use and interpret information about the vertical distribution of the canopy material.



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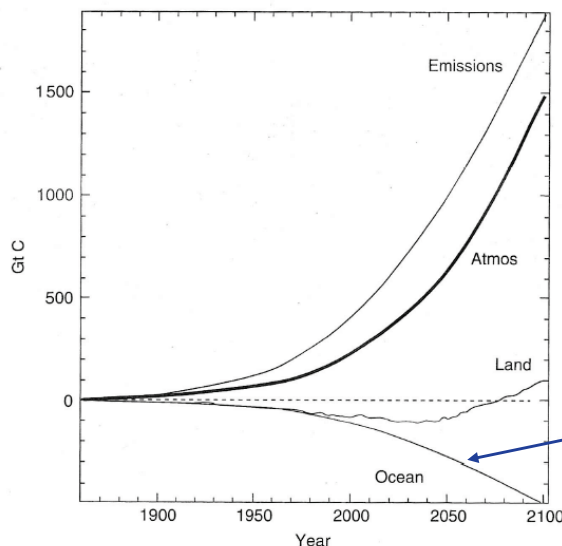
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# Uptake of Atmospheric CO<sub>2</sub> by Trees (Land Sink)

## Land sink: relatively short lived reservoir

- In this model, future water stress due to climate change eventually limits plant growth
- Feedbacks between climate change & plants could lead to almost 100 ppm additional CO<sub>2</sub> by end of century



## Ocean sink: relatively long lived reservoir

In nearly all models, ocean uptake slows relative to rise in atmospheric CO<sub>2</sub>

**Figure 3.5** Illustrating the possible effects of climate feedbacks on the carbon cycle. Results are shown of the changing budgets of carbon

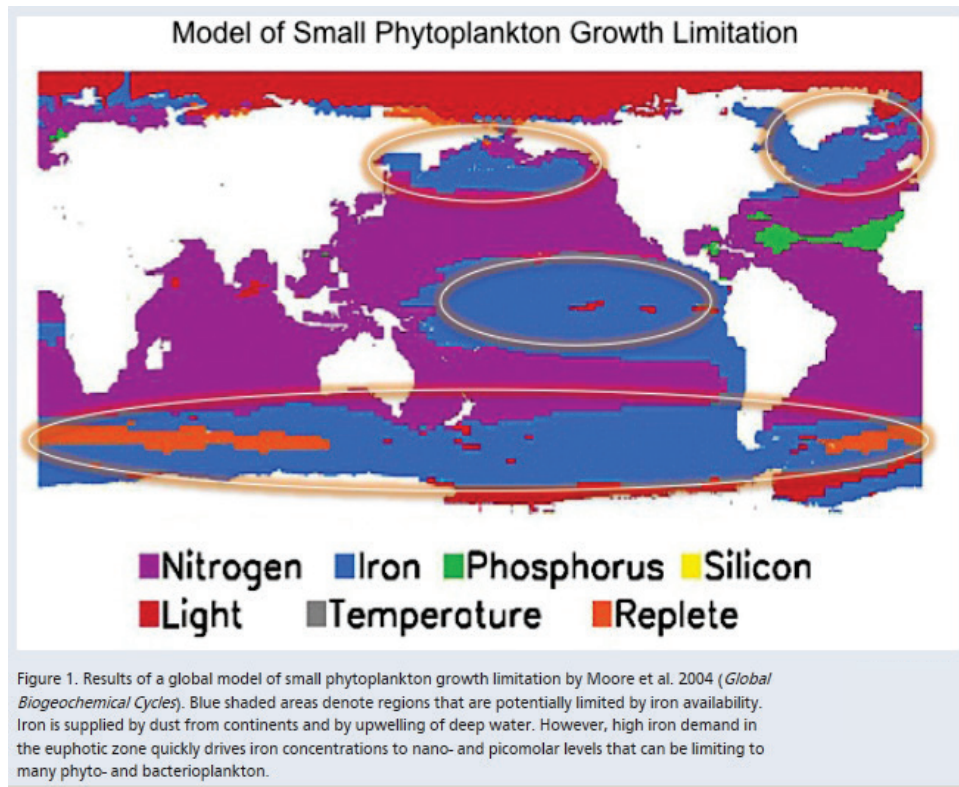
Figure 3.5, Houghton 3<sup>d</sup> Edition

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# Biology in Today's Ocean



<http://www.whoi.edu/page.do?pid=130796>

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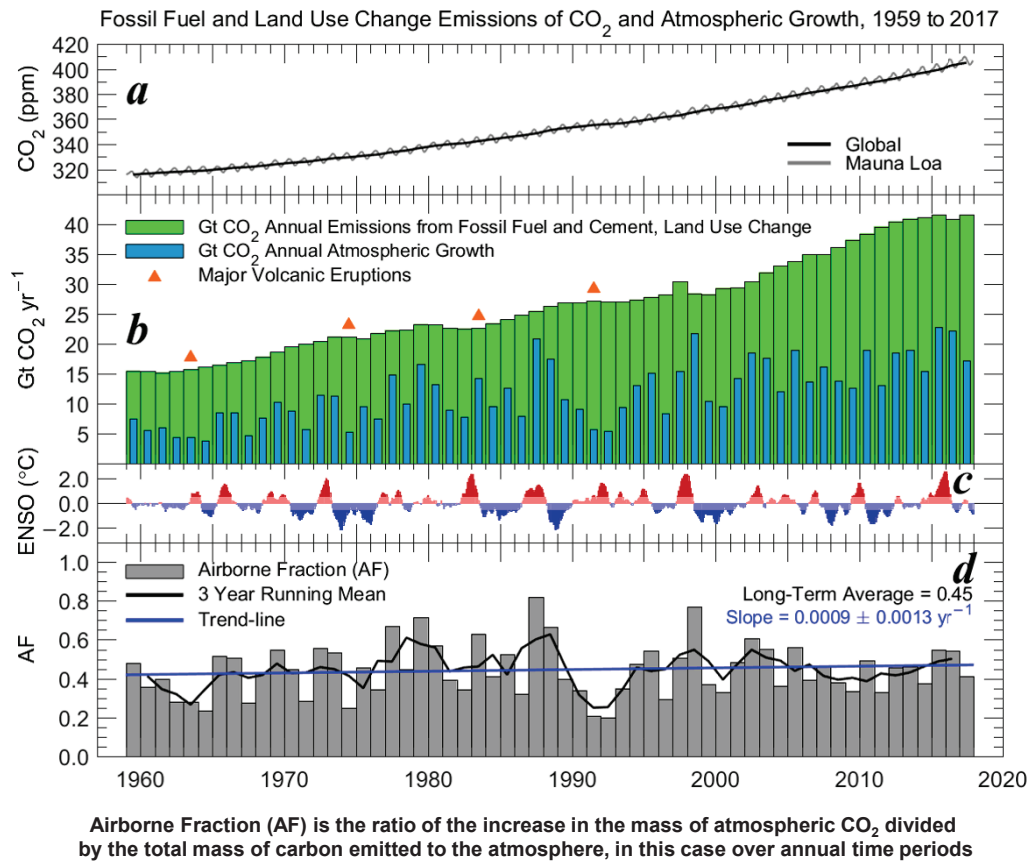


Fig 1.6 (updated & modified), *Paris Beacon of Hope*

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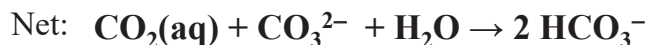
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## Uptake of Atmospheric CO<sub>2</sub> by Oceans

When CO<sub>2</sub> dissolves:



Atmospheric CO <sub>2</sub>	260 ppm Pre-Industrial	409 ppm Present Day	520 ppm 2 × Pre-Indus.
Ocean Carbon	2007 × 10 <sup>-6</sup> M	2079 × 10 <sup>-6</sup> M	2112 × 10 <sup>-6</sup> M
[HCO <sub>3</sub> <sup>-</sup> ]	1748 × 10 <sup>-6</sup> M	1881 × 10 <sup>-6</sup> M	1941 × 10 <sup>-6</sup> M
[CO <sub>2</sub> (aq)]	8.47 × 10 <sup>-6</sup> M	13.3 × 10 <sup>-6</sup> M	16.9 × 10 <sup>-6</sup> M
[CO <sub>3</sub> <sup>2-</sup> ]	251 × 10 <sup>-6</sup> M	188 × 10 <sup>-6</sup> M	155 × 10 <sup>-6</sup> M
pH	8.34	8.18	8.09

$$\text{Ocean Carbon } [\Sigma \text{CO}_2] = [\text{CO}_2(\text{aq})] + [\text{HCO}_3^-] + [\text{CO}_3^{2-}]$$

Notes:

T = 293 K; Alkalinity = 2.25 × 10<sup>-3</sup> M

M ≡ mol/liter

Mathematics supporting this calculation on Extra Slides 1 to 3

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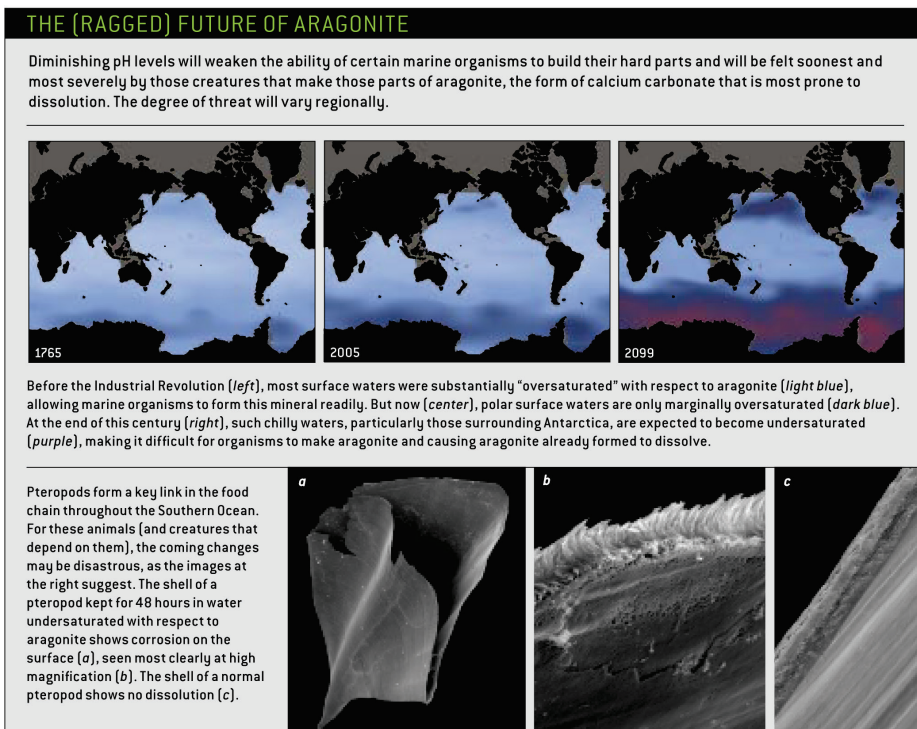
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## Uptake of Atmospheric CO<sub>2</sub> by Oceans

Oceanic uptake of atmospheric CO<sub>2</sub> leads to **ocean acidification**

**Bad news for ocean dwelling organisms that precipitate shells (basic materials)**



Doney, The Dangers of Ocean Acidification, *Scientific American*, March, 2006

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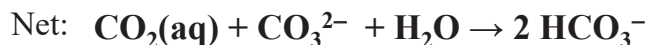
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## Uptake of Atmospheric CO<sub>2</sub> by Oceans

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pH	8.34	8.18	8.09

$$\frac{\Delta \text{Atmos}_{\text{CO}_2}}{\langle \text{Atmos}_{\text{CO}_2} \rangle_{\text{AVERAGE}}} = \frac{149 \text{ ppm}}{0.5 \times (409 + 260) \text{ ppm}} = 0.45$$

$$\frac{\Delta \text{Ocean Carbon}}{\langle \Delta \text{Ocean Carbon} \rangle_{\text{AVERAGE}}} = \frac{72 \times 10^{-6} \text{ M}}{0.5 \times (2007 + 2079) \times 10^{-6} \text{ M}} = 0.035$$

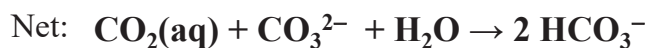
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## Uptake of Atmospheric CO<sub>2</sub> by Oceans

When CO<sub>2</sub> dissolves:



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[CO <sub>3</sub> <sup>2-</sup> ]	251 × 10 <sup>-6</sup> M	188 × 10 <sup>-6</sup> M	155 × 10 <sup>-6</sup> M
pH	8.34	8.18	8.09

$$\frac{\Delta \text{Atmos}_{\text{CO}_2}}{\langle \text{Atmos}_{\text{CO}_2} \rangle_{\text{AVERAGE}}} = \frac{111 \text{ ppm}}{0.5 \times (520 + 409) \text{ ppm}} = 0.23$$

$$\frac{\Delta \text{Ocean Carbon}}{\langle \Delta \text{Ocean Carbon} \rangle_{\text{AVERAGE}}} = \frac{33 \times 10^{-6} \text{ M}}{0.5 \times (2079 + 2112) \times 10^{-6} \text{ M}} = 0.015$$

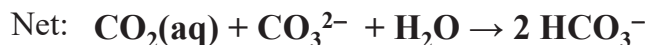
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# Uptake of Atmospheric CO<sub>2</sub> by Oceans

When CO<sub>2</sub> dissolves:



Atmospheric CO <sub>2</sub>	260 ppm Pre-Industrial	409 ppm Present Day	520 ppm 2 × Pre-Indus.
Ocean Carbon	$2007 \times 10^{-6} \text{ M}$	$2079 \times 10^{-6} \text{ M}$	$2112 \times 10^{-6} \text{ M}$
[HCO <sub>3</sub> <sup>-</sup> ]	$1748 \times 10^{-6} \text{ M}$	$1881 \times 10^{-6} \text{ M}$	$1941 \times 10^{-6} \text{ M}$
[CO <sub>2</sub> (aq)]	$8.47 \times 10^{-6} \text{ M}$	$13.3 \times 10^{-6} \text{ M}$	$16.9 \times 10^{-6} \text{ M}$
[CO <sub>3</sub> <sup>2-</sup> ]	$251 \times 10^{-6} \text{ M}$	$188 \times 10^{-6} \text{ M}$	$155 \times 10^{-6} \text{ M}$
pH	8.34	8.18	8.09

## Revelle Factor:

Although the oceans presently take up about one-fourth of the excess CO<sub>2</sub> human activities put into the air, that fraction was significantly larger at the beginning of the Industrial Revolution. That's for a number of reasons, starting with the simple one that as one dissolves CO<sub>2</sub> into a given volume of seawater, there is a growing resistance to adding still more CO<sub>2</sub>

<https://scripps.ucsd.edu/programs/keelingcurve/2013/07/03/how-much-co2-can-the-oceans-take-up>

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## Extra Slide 1

## Carbon Water Chemistry

Acidity of pure water is 7. This means  $[\text{H}^+] = 10^{-7} \text{ moles/liter}$  or  $10^{-7} \text{ M}$ .

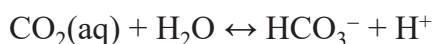
What is acidity of water in equilibrium with atmospheric CO<sub>2</sub> ?

$$[\text{CO}_2(\text{aq})] = H_{\text{CO}_2} p_{\text{CO}_2} = 3.4 \times 10^{-2} \text{ M / atm } p_{\text{CO}_2}$$

For CO<sub>2</sub> = 390 ppm:

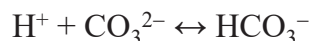
$$[\text{CO}_2(\text{aq})] = 3.4 \times 10^{-2} \text{ M / atm } 3.9 \times 10^{-4} \text{ atm} = 1.326 \times 10^{-5} \text{ M}$$

First equilibrium between CO<sub>2</sub>, HCO<sub>3</sub><sup>-</sup> (bicarbonate), and H<sup>+</sup>



$$K_1 = \frac{[\text{HCO}_3^-][\text{H}^+]}{[\text{CO}_2(\text{aq})]} = 4.3 \times 10^{-7} \text{ M (at 298 K)}$$

Second equilibrium between CO<sub>3</sub><sup>2-</sup> (carbonate), HCO<sub>3</sub><sup>-</sup>, and H<sup>+</sup>



$$K_2 = \frac{[\text{CO}_3^{2-}][\text{H}^+]}{[\text{HCO}_3^-]} = 4.7 \times 10^{-11} \text{ M (at 298 K)}$$

**Can solve if we assume charge balance:  $[\text{H}^+] = [\text{HCO}_3^-] + 2 [\text{CO}_3^{2-}]$   
- or - by taking a short-cut (see next slide)**

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## Extra Slide 2

# Carbon Water Chemistry

Acidity of pure water is 7. What is acidity of water in equilibrium with atmospheric CO<sub>2</sub> ?

Shortcut:

$$[\text{CO}_2(\text{aq})] = H_{\text{CO}_2} p_{\text{CO}_2} = 3.4 \times 10^{-2} \text{ M} / \text{atm } p_{\text{CO}_2} = 1.326 \times 10^{-5} \text{ M for present atmosphere}$$

$$[\text{H}^+] [\text{HCO}_3^-] = K_1 [\text{CO}_2(\text{aq})] = 4.3 \times 10^{-7} \text{ M} \times 1.326 \times 10^{-5} \text{ M} = 5.70 \times 10^{-12} \text{ M}^2$$

**Assume** charge balance is primarily between [H<sup>+</sup>] and [HCO<sub>3</sub><sup>-</sup>]:

$$\text{i.e., that } [\text{H}^+] \approx [\text{HCO}_3^-] \text{ and that both are } \gg [\text{CO}_3^{2-}]$$

$$[\text{H}^+] [\text{H}^+] = 5.70 \times 10^{-12} \text{ M}^2 \Rightarrow [\text{H}^+] = 2.388 \times 10^{-6} \text{ M}$$

$$\text{pH} = -\log_{10} [\text{H}^+] = \mathbf{5.6} \text{ (390 ppm, 298 K)}$$

Is the **assumption** justified? :

$$[\text{CO}_3^{2-}] = K_2 [\text{HCO}_3^-] / [\text{H}^+] \approx 4.7 \times 10^{-11} \text{ M}$$

$$[\text{H}^+] \text{ \& \ } [\text{HCO}_3^-] \text{ are both } \sim 2.4 \times 10^{-6} \text{ M which is } \gg 4.7 \times 10^{-11} \text{ M}$$

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## Extra Slide 3

# Ocean Acidity

As noted in class, the actual ocean is basic. The net charge from a series of **cations** (positively charged ions) and minor **anions** (negatively charged ions) is balanced by the total negative charge of the bicarbonate and carbonate ions. We write:

$$[\text{Alk}] = [\text{HCO}_3^-] + 2 [\text{CO}_3^{2-}] = [\text{Na}^+] + [\text{K}^+] + 2[\text{Mg}^{2+}] + 2[\text{Ca}^{2+}] - [\text{Cl}^-] - [\text{Br}^-] - 2 [\text{SO}_4^{2-}] + \dots$$

where Alk stands for Alkalinity

Henry's Law and the equations for the first and second dissociation constants yield:

$$p\text{CO}_2(\text{vmr}) = \frac{[\text{CO}_2(\text{aq})]}{\alpha} \quad K_1 = \frac{[\text{HCO}_3^-] [\text{H}^+]}{[\text{CO}_2(\text{aq})]} \quad K_2 = \frac{[\text{CO}_3^{2-}] [\text{H}^+]}{[\text{HCO}_3^-]}$$

$$\text{The three equations above can be re-arranged to yield: } p\text{CO}_2(\text{vmr}) = \left( \frac{K_2}{\alpha K_1} \right) \frac{[\text{HCO}_3^-]^2}{[\text{CO}_3^{2-}]}$$

If we substitute  $[\text{HCO}_3^-] = \text{Alk} - 2 [\text{CO}_3^{2-}]$  into the eqn above, we arrive at a quadratic eqn for  $[\text{CO}_3^{2-}]$  as a function of  $p\text{CO}_2$  and Alk. Note that  $\alpha$ ,  $K_1$ , and  $K_2$  vary as a function of temperature (T) and ocean salinity (S) (<http://en.wikipedia.org/wiki/Salinity>)

If T, Alk, & S are specified, it is straightforward to solve for  $[\text{CO}_3^{2-}]$  from the quadratic eqn.

Values for  $[\text{CO}_2(\text{aq})]$ ,  $[\text{HCO}_3^-]$ , and  $[\text{H}^+]$  are then found from Henry's law & the dissoc eqns.

Finally, Ocean Carbon is found from  $[\text{CO}_2(\text{aq})] + [\text{HCO}_3^-] + [\text{CO}_3^{2-}]$ .

Numerical values on the slides entitled "Uptake of Atmospheric CO<sub>2</sub> by Oceans" were found in this manner, using Fortran program [http://www.atmos.umd.edu/~rjs/class/code/ocean\\_carbon.f](http://www.atmos.umd.edu/~rjs/class/code/ocean_carbon.f)

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